

## TABLE OF INTEGRALS

- [1]  $\int x^n dx = \frac{1}{n+1} x^{n+1} + c, \quad n \neq -1$
- [2]  $\int \frac{dx}{x} = \ln |x| + c$
- [3]  $\int e^x dx = e^x + c$
- [4]  $\int \sin x dx = -\cos x + c$
- [5]  $\int \cos x dx = \sin x + c$
- [6]  $\int \tan x dx = \ln |\sec x| + c$
- [7]  $\int \sec^2 x dx = \tan x + c$
- [8]  $\int \operatorname{cosec}^2 x dx = -\cot x + c$
- [9]  $\int \sinh x dx = \cosh x + c$
- [10]  $\int \cosh x dx = \sinh x + c$
- [11]  $\int \tanh x dx = \ln(\cosh x) + c$
- [12]  $\int x(ax+b)^n dx = \frac{1}{a^2}(ax+b)^{n+1} \left[ \frac{ax+b}{n+2} - \frac{b}{n+1} \right] + c, \quad n \neq -1, -2$
- [13]  $\int \frac{x^2}{ax+b} dx = \frac{1}{a^3} \left[ \frac{1}{2}(ax+b)^2 - 2b(ax+b) + b^2 \ln |ax+b| \right] + c$
- [14]  $\int \frac{x^2}{(ax+b)^2} dx = \frac{1}{a^3} \left[ ax+b - \frac{b^2}{ax+b} - 2b \ln |ax+b| \right] + c$
- [15]  $\int x\sqrt{ax+b} dx = \frac{2}{a^2} \left[ \frac{(ax+b)^{5/2}}{5} - \frac{b(ax+b)^{3/2}}{3} \right] + c$
- [16]  $\int \frac{x}{\sqrt{ax+b}} dx = \frac{2ax-4b}{3a^2} \sqrt{ax+b} + c$
- [17]  $\int \frac{1}{x\sqrt{ax+b}} dx = \frac{1}{\sqrt{b}} \ln \left| \frac{\sqrt{ax+b} - \sqrt{b}}{\sqrt{ax+b} + \sqrt{b}} \right| + c, \quad b > 0$
- [18]  $\int \frac{dx}{\sqrt{a^2-x^2}} = \sin^{-1} \left( \frac{x}{a} \right) + c$
- [19]  $\int \frac{dx}{a^2+x^2} = \frac{1}{a} \tan^{-1} \left( \frac{x}{a} \right) + c$
- [20]  $\int \frac{1}{a^2-x^2} dx = \frac{1}{2a} \ln \left| \frac{x+a}{x-a} \right| + c$

$$[21] \quad \int \frac{1}{(a^2 - x^2)^2} dx = \frac{x}{2a^2(a^2 - x^2)} + \frac{1}{4a^3} \ln \left| \frac{x+a}{x-a} \right| + c$$

$$[22] \quad \int \frac{1}{x\sqrt{a^2 - x^2}} dx = -\frac{1}{a} \ln \left| \frac{a + \sqrt{a^2 - x^2}}{x} \right| + c$$

$$[23] \quad \int \frac{1}{(a^2 - x^2)^{3/2}} dx = \frac{1}{a^2} \frac{x}{\sqrt{a^2 - x^2}} + c$$

$$[24] \quad \int \frac{\sqrt{a^2 - x^2}}{x} dx = \sqrt{a^2 - x^2} - a \ln \left| \frac{a + \sqrt{a^2 - x^2}}{x} \right| + c$$

$$[25] \quad \int \frac{1}{\sqrt{x^2 \pm a^2}} dx = \ln \left| x + \sqrt{x^2 \pm a^2} \right| + c$$

$$[26] \quad \int \frac{1}{x\sqrt{x^2 + a^2}} dx = -\frac{1}{a} \ln \left| \frac{a + \sqrt{x^2 + a^2}}{x} \right| + c$$

$$[27] \quad \int \frac{1}{(x^2 \pm a^2)^{3/2}} dx = \pm \frac{1}{a^2} \frac{x}{\sqrt{x^2 \pm a^2}} + c$$

$$[28] \quad \int \sqrt{x^2 \pm a^2} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \pm \frac{1}{2} a^2 \ln \left| x + \sqrt{x^2 \pm a^2} \right| + c$$

$$[29] \quad \int \frac{\sqrt{x^2 + a^2}}{x} dx = \sqrt{x^2 + a^2} - a \ln \left| \frac{a + \sqrt{x^2 + a^2}}{x} \right| + c$$

$$[30] \quad \int \frac{1}{b + ke^{ax}} dx = \frac{1}{ab} [ax - \ln(b + ke^{ax})] + c, \quad ab \neq 0$$

$$[31] \quad \int e^{ax} \sin bx dx = \frac{1}{a^2 + b^2} e^{ax} (a \sin bx - b \cos bx) + c$$

$$[32] \quad \int e^{ax} \cos bx dx = \frac{1}{a^2 + b^2} e^{ax} (a \cos bx + b \sin bx) + c$$

$$[33] \quad \int \sin^n x dx = -\frac{1}{n} \cos x \sin^{n-1} x + \frac{n-1}{n} \int \sin^{n-2} x dx$$

$$[34] \quad \int \cos^n x dx = \frac{1}{n} \sin x \cos^{n-1} x + \frac{n-1}{n} \int \cos^{n-2} x dx$$

$$[35] \quad \int \tan^n x dx = \frac{1}{n-1} \tan^{n-1} x - \int \tan^{n-2} x dx$$

$$[36] \quad \int \sec^n x dx = \frac{\sec^{n-2} x \tan x}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2} x dx$$

$$[37] \quad \int \sin^m x \cos^n x dx = \frac{\sin^{m+1} x \cos^{n-1} x}{m+n} + \frac{n-1}{m+n} \int \sin^m x \cos^{n-2} x dx$$

$$[38] \quad \int x^n e^x dx = x^n e^x - n \int x^{n-1} e^x dx$$

$$[39] \quad \int x^n \sin x dx = -x^n \cos x + n \int x^{n-1} \cos x dx$$

$$[40] \quad \int x^n \cos x dx = x^n \sin x - n \int x^{n-1} \sin x dx$$